Quantitative Finance, Vol. 00, No. 00, July 2008, 1-23

Analysis of trade packages in Chinese stock market

Fei Ren \dagger \$\$ and Wei-Xing Zhou* \dagger \$\$

†School of Business, East China University of Science and Technology, Shanghai 200237, China ‡School of Science, East China University of Science and Technology, Shanghai 200237, China

§Research Center for Econophysics, East China University of Science and Technology, Shanghai 200237, China

(Received 00 Month 200x; in final form 00 Month 200x)

This paper conducts an empirically study on the trade package composed of a sequence of consecutive purchases or sales of 23 stocks in Chinese stock market. We investigate the probability distributions of the execution time, the number of trades and the total trading volume of trade packages, and analyze the possible scaling relations between them. Quantitative differences are observed between the institutional and individual investors. The trading profile of trade packages is investigated to reveal the preference of large trades on trading volumes and transaction time of the day, and the different profiles of two types of investors imply that institutions may be more informed than individuals. We further analyze the price impacts of both the entire trade packages and the individual transactions inside trade packages. We find the price impact of trade packages is nonnegligible over the period of the execution time and it may have a power-law relation with the total trading volume. The price impact of the transactions inside trade packages displays a U-shaped profile with respect to the time t of the day, and also shows a power-law dependence on their trading volumes. The trading volumes of the transactions inside trade packages made by institutions have a stronger impact on current returns, but the following price reversals persist over a relatively shorter horizon in comparison with those by individuals.

Keywords: Econophysics; Trade package; Stock trading behavior; Price impact; Scaling laws

*Corresponding author. Email: wxzhou@ecust.edu.cn

Quantitative Finance ISSN 1469-7688 print/ISSN 1469-7696 online © 2008 Taylor & Francis http://www.tandf.co.uk/journals DOI: 10.1080/1469768YYxxxxxxx $\mathbf{2}$

Fei Ren and Wei-Xing Zhou

1. Introduction

The study of price impact of trading on stock exchanges is known as one of the central topics in financial economics. It has been verified by many empirical studies that large trades generally have a strong impact on stock price (Ying 1966, Karpoff 1987, Wood *et al.* 1985, Gallant *et al.* 1992, Chan and Fong 2000, Lillo *et al.* 2003, Lim and Coggins 2005, Næs and Skjeltorp 2006, Zhou 2011). The single execution of a large order will lead to a large impact on stock price and increase the investor's cost. Therefore, large orders are usually split into small pieces, and executed at an extended period of time to minimize their price impact. These sequences of trades are called trade packages (Chan and Lakonishok 1995, Gallagher and Looi 2006, Giambona and Golec 2010), hidden orders (Vaglica *et al.* 2008, Moro *et al.* 2009, Vaglica *et al.* 2010), or metaorders (Farmer *et al.* 2011). Growing evidence shows that large trades play a major role in trading in stock markets, which represent a large fraction of market's total trading volume (Keim and Madhavan 1996, Jain 2003, Prino *et al.* 2007, Gregoriou 2008, Vaglica *et al.* 2010).

A large amount of research has been conducted on the large trades of institutional investors, most of which consider the individual trade as the basis unit of analysis in the study of its price impact (Keim and Madhavan 1996, Prino et al. 2007, Gregoriou 2008, Kraus and Stoll 1972, Aitken and Frino 1996, Gemmill 1996, Saar 2001, Chiyachantana et al. 2004). However, an institutional order is often broken up into a sequence of consecutive trades, and its total volume occupies a large fraction of the stock's trading volume. Therefore, it may be better to treat the sequence of trades as the basis unit of analysis in the study of institutional trades. The earliest study of trade packages may be traced back to the study by Chan and Lakonishok (1995). They analyze the price impact of the entire sequence of trades in Now York and American Stock Exchanges, and find that the price impact is related to package size and trade complexity. Gallagher and Looi (2006) study the abnormal returns for trade packages of the Australian equity managers to estimate their trade performance. Giambona and Golec (2010) study the wrong trades inside trade packages by large intuitional insider. Recently, Vaglica et al. (2008), Moro et al. (2009), and Vaglica et al. (2010) try to study the market impact of trade packages identified by the continuous increase or decrease of a firm's stock inventory. Farmer et al. (2011) propose a theoretical model to study the permanent impact of large trading orders. The application of such research lies in the study of optimal execution of large orders to minimize the trading costs of institutional investors (Almgren 2003, Obizhaeva and Wang 2010, Alfonsi et al. 2010).

Many articles have addressed the question of how to measure the price impact of trade packages. Chan and Lakonishok (1995) study the price impact during trade packages using the average, open and close price on the first and last day of the trade package. Following their works, Gallagher and Looi (2006) measure the impact over an extended period of time before the start and after the end of the package. Instead, Vaglica *et al.* (2008), Moro *et al.* (2009), and Vaglica *et al.* (2010) study the price impact of trade packages using the transaction data, measured as the difference between the prices of the fist and last transaction of the trade package.

In this paper, we are not only interested in the market impact of the entire trade package, but also concerned about the impact of the individual transactions inside packages. For the study of price impact of isolated large trades, an early study measures the price impact using the close price a few days before and after the trades (Kraus and Stoll 1972). Keim and Madhavan (1996) use the close price on the trading day prior to and after block trades. In stead of using the close price, recent studies choose the transaction price to estimate the price impact of individual trades, e.g., the average price of several transactions prior to and after block trades (Prino *et al.* 2007, Gemmill 1996), or the transaction price immediately prior to and after block trades (Gregoriou

2008).

To the best of our knowledge, the empirical study on trade packages in Chinese stock market has not been conducted. This may due to the difficulty of collection of proprietary data. We have the ultrahigh-frequency data of 23 liquid stocks on the Shenzhen Stock Exchange in year 2003. The data contain the information about all the transactions of each investor, including the trading price, the trading volume, the transaction time, etc. We use the trading records of the 23 stocks as our sample data, and analyze the price impact of trade packages and the individual transactions inside using the transaction price.

Unlike the data provided by the Plexus Group (Keim and Madhavan 1995.Chiyachantana et al. 2004), we are not directly informed of the large institutional trades from our database. Proxy methods are used to detect the trade packages, for instance, a technical detection algorithm based on the inventory time evolution of firms (Vaglica et al. 2008, Moro et al. 2009, Vaglica et al. 2010). In the present work, we follow the ideal introduced in Chan and Lakonishok (1995), Gallagher and Looi (2006) and Giambona and Golec (2010), and define the trade package as a sequence of mostly buy or sell trades with less than a n-day break between chronologically adjacent trades. Consistent with the results revealed in previous studies, we observe similar results for various length of break n = 1, 5, 10 days, other than some quantitative differences.

So far, previous studies of trade packages primarily focus on the large trades made by institutional investors. Our database includes the trading records for both institutional and individual investors, identified by a particular code denoting the investor type. Large trades made by individuals, e.g., private equity investments, can also be detected using the same detection rules. Therefore, we can also study the price impact of large individual trading. In addition, our present study further confirms the nonlinear power-law relation between the price returns and trading volumes, as revealed in many empirical studies (Hasbrouck 1991, Plerou *et al.* 2002, Chordia and Subrahmanyam 2004, Zhou 2011). Another purpose is to study the price impact of individual transactions inside trade packages. We find that the individual transactions have a strong positive impact on the current price and a temporary negative impact on the following prices, though the cumulative impact of the entire trade package is nonnegligible over the whole period of execution time.

The remainder paper is organized as follows. In Section 2, we introduce our database, the investigated variables of trade packages and their summary statistics. Sections 3 studies the statistic properties of trade packages, including the probability distributions of the investigated variables and their scaling relations. In Section 4, we attempt to study the trading profile of trade packages by analyzing the mean trading volume, transaction probability and the total trading volume with respect to the time of a day. The price impacts of the entire trade packages and the individual transactions inside trade packages are carefully studied in Section 6. Section 7 summarizes our findings.

2. Data and investigated variables

2.1. Data sample

The data used in our study comprise 23 liquid stocks traded on the Shenzhen Stock Exchange (SZSE), one of the two stock exchanges in mainland China. The SZSE was established on December 1, 1990 and started its operations on July 3, 1991. The SZSE has two separate markets including A-shares and B-shares. A-shares are common stocks issued by mainland Chinese companies, subscribed and traded in Chinese currency *Renminbi* (RMB), purchased and sold by

4

Chinese nationals and approved foreign investors. The A-share market was launched in 1990 and opened only to domestic investors before 2003. B-shares are also issued by mainland Chinese companies, but traded in foreign currencies. B-shares carry a face value denominated in RMB. The B-share Market was launched in 1992 and was restricted to foreign investors before February 19, 2001. It has been opened to Chinese investors since then.

We mainly study the data of 23 stocks in A-share market of the SZSE in year 2003. Up to the end of 2003, there have been 491 A-share stocks listed on the SZSE. The total market capitalization of A-share market was 1.2 billion RMB and the float market capitalization was 0.45 billion RMB. Our sample stocks were part of the 40 constituent stocks composing the Shenzhen Stock Exchange Component Index in 2003. These 23 stocks are representative in a variety of industry sectors, as shown in Table 1. The total transaction amount A_{tot} , the float capitalization C_{flo} and the total market capitalization C_{tot} , in unit of million RMB, of 23 stocks in year 2003 are also listed in Table 1. For instance, the total transaction amount A_{tot} of stock 000001 in 2003 is 23847.6 million RMB, and the float capitalization C_{flo} and total market capitalization C_{tot} of the same stock are 12 and 16.6 million RMB respectively. The A_{tot} is three orders of magnitude larger than C_{flo} and C_{tot} . Similar phenomenon are observed in all the 23 stocks, which implies that the average transaction amount per day of a certain stock almost approximates to its total market capitalization. This indicates that the market was relatively active in 2003, though it was in the middle of a five-year bear market (Zhou and Sornette 2004).

The SZSE generally opens from Monday to Friday, but closes for public holidays and other dates as announced by the China Securities Regulatory Commission. We mainly consider the continuous double auction operates from 9:30 to 11:30 and 13:00 to 15:00. Based upon the orders of submission and cancelation, the transaction is automatically executed according to price-time priority matching rule. The trading records of 23 stocks are consequently extracting from the original database of order flows. It is worthwhile to point out that the account number for each investor is provided under the condition that the name of the investor involved is removed from the data. Therefore, we can obtain the sequence of transactions for each investor, which contains the information about the trade price, the trading volume, and the transaction time. We treat those transactions executed by a certain investor at the same time but traded with different investors as one trade for this investor. Moreover, in our database each market member is endowed with a code identifying the investor type, i.e., institution and individual. That makes it possible to compare the trading dynamics between those two types of investors.

Table 1 presents summary statistics of the trading records of 23 stocks, including the number of investors N_{inv} , the total number of trades N_{tra} , the mean, median and standard deviation of the number of trades per investor. The number of investors N_{inv} varies in the range from 34814 (stock 000720) to 533752 (stock 000001), and the total number of trades N_{tra} varies in the range from 194644 (stock 000541) to 2925841 (stock 000001). We integrate the trading records of the 23 stocks, and the sample size is 18597649 trades in total. For most of the stocks analyzed in our study, the mean number of trades for each investor is around 5, and the median is slightly smaller, about 2 or 3. The standard deviation of the number of trades per investor fluctuates in a wide range between 9.3 and 35.4, and the large values of the standard deviation indicate big differences between the trades number of different investors.

2.2. Identification of trade packages

The trade package is defined as a sequence of mostly buy (sell) trades of a stock, and it is generally ended by a specific break time between chronologically adjacent trades. The selection of the break time does not sensitively affect the results, only brings a quantitative difference. Giambona and Golec (2010) use an eight-day break to analyze the trade package made by Gabelli

Table 1. Summary statistics of the trading records of 23 stocks traded on Shenzhen Stock Exchange. The basic information about the 23 stocks includes the stock code and industry they belonging to. We present the summary statistics for each stock, i.e., the total transaction amount A_{tot} , the float capitalization C_{flo} , the total market capitalization C_{tot} , the number of investors N_{inv} , the total number of trades N_{tra} , the mean, median and standard deviation of the number of trades per investor.

						Numbe	er of trades	per investor	
Code	A_{tot}	C_{flo}	C_{tot}	N_{inv}	N_{tra}	Mean	Median	Std. dev.	Industry
000001	23847.6	12.0	16.6	533752	2925841	5.5	3	20.9	Financials
000002	13024.6	6.1	7.5	299507	1640238	5.5	3	24.4	Real estate
000009	6287.8	2.6	4.3	261927	1459247	5.6	3	15.2	Conglomerates
000012	6009.0	0.8	2.8	110038	859938	7.8	3	27.2	Metals & Nonmetals
000016	2981.1	1.5	2.7	110641	563163	5.1	2	19.6	Electronics
000021	8200.8	2.2	8.0	202049	1258294	6.2	3	21.3	Electronics
000024	2714.6	1.9	4.2	80894	389260	4.8	2	15.6	Real estate
000027	8486.3	4.4	10.9	218796	1038232	4.7	2	27.2	Utilities
000063	10436.5	4.7	12.5	127302	799601	6.3	3	35.2	IT
000066	4255.2	1.5	3.8	144863	845377	5.8	3	14.2	Electronics
000088	4196.7	3.0	13.9	53420	270488	5.1	2	22.2	Transportation
000089	5821.2	2.7	7.4	102153	577781	5.7	3	27.4	Transportation
000406	5197.4	2.2	3.0	152491	832141	5.5	3	14.9	Petrochemicals
000429	1787.8	1.4	4.7	77888	352044	4.5	2	9.3	Transportation
000488	3876.8	2.4	5.3	54315	347032	6.4	3	35.4	Paper & Printing
000539	4840.5	4.2	21.4	61142	317321	5.2	2	20.6	Utilities
000541	1629.9	1.8	3.3	42290	194644	4.6	2	21.2	Electronics
000550	7908.4	1.2	5.4	165980	1036314	6.2	3	24.9	Manufacturing
000581	3031.0	2.5	4.0	60790	283199	4.7	2	22.6	Manufacturing
000625	14063.8	2.5	13.3	156825	1150636	7.3	3	28.0	Manufacturing
000709	4155.7	3.0	10.2	138621	650911	4.7	2	23.0	Metals & Nonmetals
000720	3684.2	4.9	8.5	34814	332141	1 9.5 5 16.2 U		Utilities	
000778	4536.7	2.5	7.0	91802	473806	5.2	2	21.8	Manufacturing

asset management company, and they find that the package groupings are not sensitive to the length of the break. In fact, there is no much difference observed for the break length longer than 5 days, as shown in the following context. In this paper, we present the results of trade packages ended by the break of 1,5,10 days separately.

Denote v_i as the trading volume of a certain transaction *i* inside a trade package, we consider the trade package consisted mostly of purchases or sales, i.e., $\frac{\sum_{buy} v_i}{\sum v_i} > \theta$ or $\frac{\sum_{sell} v_i}{\sum v_i} > \theta$. The parameter θ is set to be 0.75 in the present study. For other values $\theta > 0.75$ we observe similar results, consistent with the results found by Vaglica *et al.* (2008). The investors, who occasionally trade in stock market, may have packages containing very few trades which also satisfy the above condition. To avoid considering those investors who are unlikely to split their trades, we choose relatively active investors and restrict the packages with $N_m > 5$, where N_m is the number of trades done through market orders. Market orders are submitted by investors who are urgent to trade, and are executed immediately after the submission. Those orders waited in the limit order book and executed later are limit orders. The threshold 5 is close to the mean number of trades per investor shown in Table 1. If a package of trades has N_m larger than the mean number of trades per investor, we regard it to be a trade package made by an active investor.

Following the detecting rules: (i) packages are separated by a n-day break, (ii) at least 75% of the trading volumes in the package are buying or selling volumes, (iii) the number of trades executed as market orders in the package should be larger than 5, we find out the trade packages of 23 stocks. We integrate the package samples over all the 23 stocks. As shown in Table 2, there are 1187, 1066, 923 trade packages made by institutions detected for the break of 1, 5, 10 days.

6

Fei Ren and Wei-Xing Zhou

For individuals, the number of trade packages detected is larger, 35187, 37924, 35319 for the break of 1, 5, 10 days. This may because that the number of individual investors is much larger than the number of institutional investors. There are 3215246 individuals and 67054 institutions traded in the 23 stocks in year 2003. This may also be explained by their different ways of trading in stock market. Institutions trade strictly following their trading strategies, and they do not trade as frequently as individuals.

The variables characterizing the trade packages are defined as following: (i) The execution time T of the trade package, measured as the interval between the first and last transaction of the trade package, in unit of one second. (ii) The number of trades N within the trade package. (iii) The total trading volume of the trade package, denoted as $V = \sum_{i=1}^{N} v_i$. Table 2 gives the means of the execution time, the number of trades and the total trading

Table 2 gives the means of the execution time, the number of trades and the total trading volumes for both institutions and individuals. The mean of the execution time $\langle T \rangle$ shows an increasing tendency as the increase of the break time separating packages. It is 5973, 57259, 113779 seconds for institutions, and 5553, 58701, 117811 seconds for individuals for the break of 1, 5, 10 days. The mean of the number of trades $\langle N \rangle$ for institutions is 41, 54, 56 for the break of 1, 5, 10 days, larger than 32, 35, 36 those for individuals. Similarly, the mean of the total trading volumes $\langle V \rangle$ for institutions is 177311, 224872, 236013 for the break of 1, 5, 10 days, larger than 121841, 124456, 124004 those for individuals. This implies the institutions have capitalization on average larger than individuals, and need more transactions to accomplish the purchase or sale of large amounts of shares. In general, a trade package consists of a sequence of 30 - 60 consecutive transactions, and each transaction on average has 4000 shares. Therefore, the trade packages analyzed in our study are of extremely large size.

3. Statistics properties of trade packages

3.1. Probability distributions of variables characterizing trade packages

Vaglica *et al.* (2008) study three most capitalized stocks traded on the Spanish Stock Exchange (BME), and reveal that the probability distribution functions (PDFs) of the variables T, N and V have power-law tails with exponents lying in an interval [1.2, 2.3]. An extended study of 23 stocks on BME and 74 stocks on the London Stock Exchange (LSE) further confirms this result (Moro *et al.* 2009). We pool together the data from 23 stocks on the SZSE, and investigate the PDFs of T, N and V for trade packages ended by the break of 1,5,10 days. Power-law tails are observed in the PDFs of these variables. For a variable x which obeys a power-law tail distribution, we suppose its PDF follows a formula

$$P(x) = cx^{-\delta}, \ x \ge x_{\min}.$$
 (1)

We first calculate the PDF of the execution time T. Note the PDF is different for different types of investors, we present the results for institutions and individuals respectively. In Figures 1(a) and 1(b), P(T) of trade packages ended by the break of 1,5,10 days for both institutions and individuals are plotted. The PDFs seem to have power-law tails, and we fit them using a powerlaw function presented in Equation (1). A rough estimation shows the exponent δ might smaller than one. For a sequence of variable $x = x_1, \dots, x_n$ restricted to a finite region $[x_{\min}, x_{\max}]$, the parameter c is

$$c = \frac{1 - \delta}{x_{\max}^{1 - \delta} - x_{\min}^{1 - \delta}},\tag{2}$$

1:9

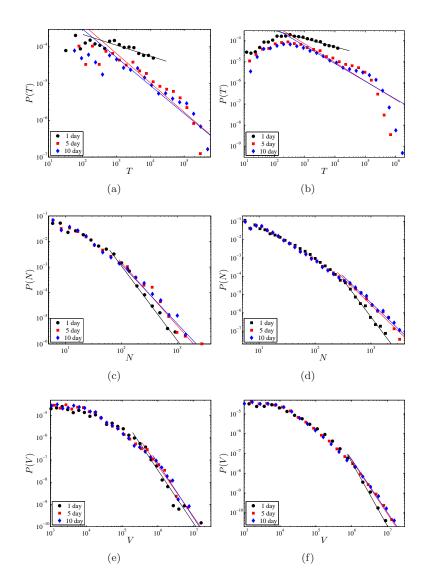


Figure 1. (Color online) Probability distribution functions (PDFS) of the variables characterizing the trade packages with various break length n = 1, 5, 10 days using the aggregated data from the 23 stocks: (a) PDF of the execution time T for institutions, (b) PDF of the execution time T for individuals, (c) PDF of the number of trades N for institutions, (d) PDF of the number of trades N for individuals, (e) PDF of the trading volume V for institutions, and (d) PDF of the trading volume V for individuals. The solid curves are power-law fits with exponents depicted in Table 2.

under the normalization condition $\int_{x_{\min}}^{x_{\max}} p(x) dx = 1$. To obtain the maximum likelihood estimate of the exponent δ , one needs to solve the equation

$$\frac{\partial L}{\partial \delta} = \frac{n}{\delta - 1} - n \frac{x_{\min} \ln x_{\min} x_{\max}^{\delta} - x_{\max} \ln x_{\max} x_{\min}^{\delta}}{x_{\max} x_{\min}^{\delta} - x_{\min} x_{\max}^{\delta}} - \sum_{i=1}^{n} x_i = 0,$$
(3)

Following the work by Clauset et al. (2009), we use an efficient method of fitting power-law

8

Fei Ren and Wei-Xing Zhou

distributions based on the Kolmogorov-Smirnov (KS) statistic to estimate the parameters in Equation (1). The KS statistic is defined as

$$KS = \max_{x \ge \hat{x}_{\min}} \left(|F - F_{\text{PL}}| \right), \tag{4}$$

where F is the cumulative distribution function (CDF) of the empirical data and F_{PL} is the CDF of the power-law fit. The CDF of the power-law function in Equation (1) with parameter c in Equation (2) is

$$F_{\rm PL}(x) = 1 - \frac{1 - x_{\min}^{\delta - 1} x^{1 - \delta}}{1 - x_{\min}^{\delta - 1} x_{\max}^{1 - \delta}}.$$
(5)

To make the empirical PDF and the best power-law fit as similar as possible, we determine the estimate of \hat{x}_{\min} by minimizing the KS statistic, then we estimate the exponent δ by solving Equation (3). The parameter c is obtained by substituting \hat{x}_{\min} and δ into Equation (2). The standard error on δ , according to Clauset *et al.* (2009), is

$$\sigma = -\frac{1}{nE\left[\frac{\partial^2 L}{\partial \delta^2}\right]}.$$
(6)

As shown in Figure 1(a), P(T) for institutions displays power-law tails covering a scaling range over two orders of magnitude, and the exponent δ_T varies with different break length. For the break of one day, δ_T is estimated to be 0.3, while for the break longer than five days δ_T is relatively constant and is around 0.8. In the figure, the power-law fits with parameters listed in Table 2 are also illustrated. For individuals, we observe similar results, and the estimated values of δ_T are slightly larger than those for the institution, as depicted in Table 2.

We then calculate the PDF of the number of trades N. In Figures 1(c) and 1(d), we plot P(N) of trade packages ended by the break of 1,5,10 days for both institutions and individuals. It also has power-law tails, but with exponent δ_N obviously greater than 1.0. For $\delta > 1.0$, the parameter c in Equation (1) in the limit of $x_{max} \to \infty$ approximates

$$c = \frac{\delta - 1}{x_{\min}^{1 - \delta}},\tag{7}$$

and the exponent is

$$\hat{\delta} = 1 + n \left(\sum_{i=1}^{n} \ln \frac{x_i}{x_{\min}}\right)^{-1}.$$
(8)

This formula is the same as that proposed by Clauset *et al.* (2009). We use the same power-law fitting method based on KS statistic to estimate the parameters \hat{x}_{\min} and δ . Now the CDF of the power-law fit with $\delta > 1.0$ is

$$F_{\rm PL}(x) = 1 - \left(\frac{x_{\rm min}}{x}\right)^{\delta - 1}.$$
(9)

The standard error on δ is obtained according to Equation (6).

The power-law exponent δ_N varies with different break length. For institutions, δ_N is estimated

Table 2. Summary properties of trade packages of the aggregated data from the 23 stocks. The results are presented for trade packages made by institutions and individuals with various break length n = 1, 5, 10 days. N_p is the number of $(N_p) = (N_p) = 1 - (N_p)$

packages, $\langle T \rangle$, $\langle N \rangle$ and $\langle V \rangle$ are means of the execution time, the number of trades and the total trading volumes. The power-law exponents δ_T , δ_N and δ_V are obtained by fitting Equation (1) estimated by a maximum with the second second

obtained by fitting Equation (1), estimated by a maximum likelihood method based on KS statistic. The exponents g_1 , g_2 and g_3 describe the scaling relations in Equation (10).

		Institution		_		Individual	
	1 day	5 days	10 days		1 day	$5 \mathrm{days}$	10 days
N_p	1187	1066	923		35187	37924	35319
$\langle T \rangle$	5973	57259	113779		5553	58701	117811
$\langle N \rangle$	41	54	56		32	35	36
$\langle V \rangle$	177311	224872	236013		121841	124456	124004
δ_T	0.30 ± 0.03	0.80 ± 0.01	0.77 ± 0.01		0.39 ± 0.005	0.88 ± 0.002	0.84 ± 0.002
δ_N	2.92 ± 0.13	2.47 ± 0.12	2.31 ± 0.11		4.06 ± 0.19	2.94 ± 0.09	2.92 ± 0.09
δ_V	2.40 ± 0.08	2.31 ± 0.10	2.47 ± 0.17		3.23 ± 0.08	2.73 ± 0.09	2.69 ± 0.09
g_1	0.18 ± 0.05	0.49 ± 0.08	0.49 ± 0.16		0.13 ± 0.03	0.38 ± 0.05	0.34 ± 0.06
g_2	0.74 ± 0.08	0.77 ± 0.05	0.77 ± 0.07		0.72 ± 0.07	0.79 ± 0.08	0.80 ± 0.08
g_3	0.18 ± 0.08	0.51 ± 0.17	0.53 ± 0.15		0.16 ± 0.03	0.56 ± 0.07	0.43 ± 0.04

to be 2.9 for the break of one day, and about 2.4 for the break longer than five days. For individuals, δ_N is 4.0 for the break of one day, and about 2.9 for the break longer than five days. The power-law fits are also illustrated in the figure, and the estimated values of δ_N are depicted in Table 2.

We also calculate the PDF of the total trading volume V, and similar power-law tails are observed. In Figures 1(e) and 1(f), P(V) of trade packages ended by the break of 1,5,10 days for both institutions and individuals are plotted. For institutions, δ_V for the break of one day is 2.4, displaying a value very close to that for the break longer than five days, while for individuals δ_V for the break of one day is 3.2 larger than 2.7 that for the break longer than five days. The power-law fits of P(V) with parameters listed in Table 2 are also illustrated in the figure.

3.2. Scaling relations between variables characterizing trade packages

Empirical studies have revealed that there exist scaling relations between variables T, N and V

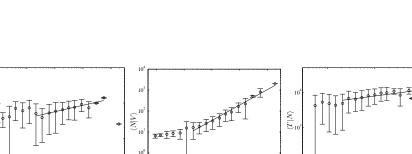
$$T \sim V^{g_1}, \quad N \sim V^{g_2}, \quad T \sim N^{g_3}.$$
 (10)

It is found $g_1 \simeq 2$, $g_2 \simeq 1$, and $g_3 \simeq 1.7$ for BME and LSE markets (Moro *et al.* 2009). We also find that T, N and V of the trade packages for SZSE are related through scaling relations, but with different values of g_1 , g_2 and g_3 , primarily due to the small value of the exponent δ_T . Since the exponents δ_T , δ_N and δ_V differ for the two types of investors, we calculate the scaling relations for institutions and individuals respectively.

We study the scaling relation between T and V by calculating the mean conditional execution time $\langle T|V\rangle$ conditioned on the total trading volume V. We arrange the entire T sequences in ascending order, and partition it to 20 bins with equal size. We calculate $\langle T|V\rangle$ conditioned on a bin of V to get better statistics. In Figure 2(a), $\langle T|V\rangle$ for trade packages of institutions ended by the break of one day is plotted. For large scales of V, one observes a scaling relation between Tand V, and g_1 is estimated to be 0.18. This is consistent with the previous result that P(V) obeys $\langle T | V \rangle$

Fei Ren and Wei-Xing Zhou

Trading package v3



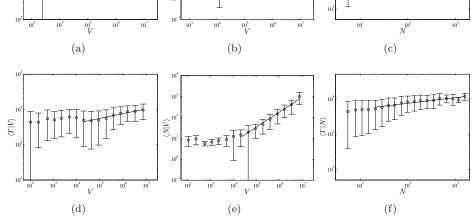


Figure 2. (Color online) Scaling relations between the variables characterizing the trade packages with break length n = 1 day: (a) mean conditional execution time $\langle T|V \rangle$ for institutions, (b) mean conditional number of trades $\langle N|V \rangle$ for institutions, (c) mean conditional execution time $\langle T|N \rangle$ for institutions, (d) mean conditional execution time $\langle T|V \rangle$ for individuals, (e) mean conditional number of trades $\langle N|V \rangle$ for individuals, and (f) mean conditional execution time $\langle T|N \rangle$ for individuals. The solid curves are power-law fits with exponents depicted in Table 2.

power law for large V. We also study the scaling relations between N and V, T and N using the same method, and obtain $g_2 = 0.74$ and $g_3 = 0.18$ as illustrated in Figures 2(b) and 2(c). For trade packages of individuals ended by the break of one day, we obtain $g_1 = 0.13$, $g_2 = 0.72$ and $g_3 = 0.16$, slightly smaller than those for institutions, as shown in Figures 2(d), 2(e) and 2(f). Similar results are observed for trade packages of both institutions and individuals ended by the break longer than five days. According to the scaling relations in Equation (10), one can infer the relation that $g_1 = g_2g_3$. The estimated values of g_1 , g_2 and g_3 depicted in Table 2 prove the inferred relation between them.

4. Trading profile

We further consider the question of how the individual transactions inside trade packages are executed as a function of the time t of a day, which is called trading profile. We are mainly concerned about the trade packages finished within one day, i.e., packages ended by the break of one day, and the time t is normalized by the time of a trading day D = 14400 seconds. Denote v_i as the trading volume of transaction i inside trade packages, we calculate the mean volume of each transaction $\langle v(t) \rangle$ traded at normalized time t/D. To make the trading volumes of different stocks comparable, v_i of a particular stock is normalized by its mean value.

In Figures 3(a) and 3(b), the mean trading volume $\langle v(t) \rangle$ of individual transactions inside trade packages is plotted as a function of the normalized time t/D for institutions and individ-

uals respectively. Since the mean trading volume may differ for the transactions with different aggressiveness, we calculate $\langle v(t) \rangle$ of the transactions executed as market orders (filled black circles) and limit orders (empty black circles). One observes that institutions prefer to place large market orders close to the opening time, while individuals are more likely to place large market orders close to the closing time of the day. Moreover, $\langle v(t) \rangle$ of market orders is much more significant than that of limit orders, which indicates that the trade packages are accomplished mostly by market orders. Therefore, $\langle v(t) \rangle$ of the total market orders and limit orders (black squares) shows a similar profile to that of the market orders. The mean trading volume of the transactions concurrently traded with trade packages (red diamonds) also has a similar profile, slightly larger than that for the total market orders and limit orders, different from that observed in BME and LSE markets (Clauset *et al.* 2009). These results are quite robust for trade packages of both institutions and individuals.

To complectly understand the trading profile, we further consider the number of transactions executed at time t. We calculate the probability distribution P(t) of the transaction time t, defined as the proportion between number of transactions traded at time t to the total number of transactions inside trade packages. As shown in Figure 3(c), P(t) for institutions is relatively small close to the opening time of the day. It may be explained by the phenomena that the mean volume of individual transactions is significant large then, and only a few numbers of transactions could accomplish the purchase or sale of large amounts of shares. There is a midday break during the lunch time in Chinese stock market, and the surge of P(t) soon after midday break may be caused by the entrance of many institutions who start trade packages in the afternoon. An increase of P(t) is also observed close to the closing time of the day, this may because that all the trade packages within one day should be accomplished at that time. The probability distribution P(t) for individuals shows a similar profile to that for institutions. We also measure the probability distribution of the initial and final time of trade packages. As shown in Figures 3(e) and 3(f), for both institutions and individuals a significant fraction of trade packages are started at the opening time and finished at the closing time. Moreover, there are quite a number of trade packages start after the midday break, and this may explain the surge of P(t) soon after the midday break.

We finally investigate the total trading volume of individual transactions inside trade packages traded at time t, i.e., the product of the mean volume of individual transactions and the number of transactions. In Figures 3(g) and 3(h), the total trading volume $\sum v(t)$ of transactions inside trade packages is plotted with respect to time t for institutions and individuals respectively. For the opening hours in the morning, $\sum v(t)$ for institutions shows a maximum at around 0.1 day (approximately at 10:00), about half hour earlier than the location of the maximum for individuals. After the midday break, $\sum v(t)$ for institutions shows a rapid increase and exhibits a maximum at round 0.65 day (approximately at 13:30), while no such peak is observed for individuals. Large $\sum v(t)$ is further observed close to the closing time for both institutions and individuals. The fact that institutions start their trade packages earlier than individuals implies institutions may be more informed than individuals.

5. Price impact

5.1. Price impact of trade packages

The price impact is a very important issue in financial studies, and a large number of studies have focused attention on this topic. In this section, we first consider the price impact of trade packages, generally measured as the difference between the price prior and after the trade pack-

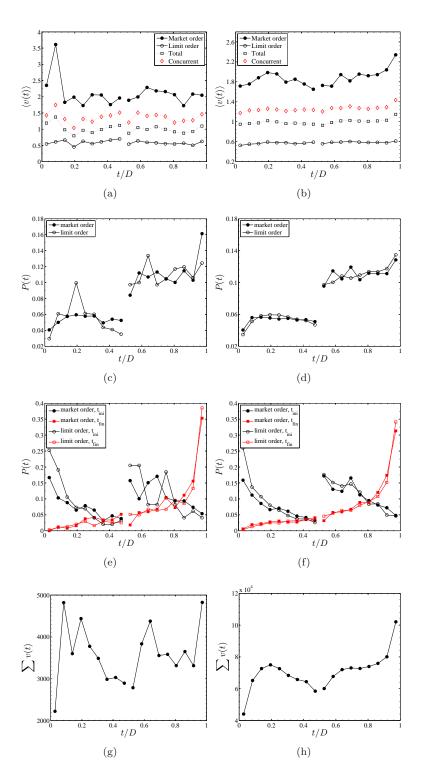


Figure 3. (Color online) Trading profile of trade packages finished within one day: mean trading volume $\langle v(t) \rangle$ for (a) institutions and (b) individuals, probability distributions of the transaction time t for (c) institutions and (d) individuals, probability distributions of the initial time t_{ini} and final time t_{fin} for (e) institutions and (f) individuals, and total trading volume $\sum v(t)$ for (g) institutions and (h) individuals. The time t is measured with respect to the time of a day.

age (Chan and Lakonishok 1995, Gallagher and Looi 2006). For a trade package accomplished between time t and t + T, we follow the work by Moro *et al.* (2009), and define the price impact as the difference between the logarithmic price of the first and last transaction of the trade package

$$r = \ln p(t+T) - \ln p(t).$$
(11)

The scaled price impact is obtained by taking into account the normalization condition and the sign of the trade package

$$R = sr/\langle |r| \rangle,\tag{12}$$

where s = +1 (-1) represents the package with mostly buy (sell) trades, and r is normalized by the mean absolute return $\langle |r| \rangle$ of the relevant stock.

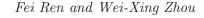
5.1.1. R vs T

We investigate the dependence of the scaled price impact R on the execution time T. We only consider the trade packages finished within one day, since the price impact persists over more than one day not only capture the information contained in the trade package but also be affected by the nonsuccessive trades overnight. In Figures 4(a) and 4(b), the mean conditional scaled price impact $\langle R|T \rangle$ is plotted as a function of the execution time T for institutions and individuals respectively. A trade package can be accomplished with different component of market orders and limit orders. To identify it, we calculate the variable F_m defined as the fraction of volumes done through market orders within trade packages. The mean conditional price impact $\langle R|T \rangle$ for trade packages with large and small fraction of market orders, i.e., $F_m > 0.8$ and $F_m < 0.2$, are represented separately in the figure.

Despite of strong fluctuation in the conditional price impact, the mean conditional price impact $\langle R|T\rangle$ with $F_m > 0.8$ is mostly positive over the whole range of T for both institutions and individuals. This indicates that the trade package has a nonnegligible price impact over the whole range of execution time up to one day. The cumulative effect of a sequence of mostly buyer-initiated trades is more like to raise the price, while the cumulative effect of a sequence of mostly seller-initiated trades is more likely to reduce the price. Moreover, $\langle R|T\rangle$ with $F_m < 0.2$ is mostly negative, and this implies that the price impact of a trade packages is not dominated by the sign of the most trades when there is a low fraction of market orders. We further perform the analysis of variance (ANOVA) to test if the means of the conditional price impact for different T are equal. For institutions, we obtain a p-value 0.919 for trade packages with $F_m > 0.8$, and a p-value 0.787 for trade packages with $F_m < 0.2$. Similar large p-values are observed for trade packages of individuals, which indicates that $\langle R|T\rangle$ does not have much difference for various T. No clear tendency of $\langle R|T\rangle$ is observed in our study.

5.1.2. R vs V

We then investigate the dependence of the scaled price impact R on the total trading volume V. The mean conditional scaled price impact $\langle R|V\rangle$ with $F_m > 0.8$ and $F_m < 0.2$ for both institutions and individuals are plotted as a function of the total trading volume V in Figures 4(c) and 4(d). For both institutions and individuals, $\langle R|V\rangle$ is mostly positive for trade packages with $F_m > 0.8$, while mostly negative for trade packages with $F_m < 0.2$. This further confirms our previous finding that the cumulative impact of a trade package is dominated by the sign of the most trades when there is a large fraction of market orders. We also use the ANOVA to compare the means of the conditional price impact for different V, and find very small p-values for trade packages of both institutions and individuals with $F_m > 0.8$ and $F_m < 0.2$, indicating the means



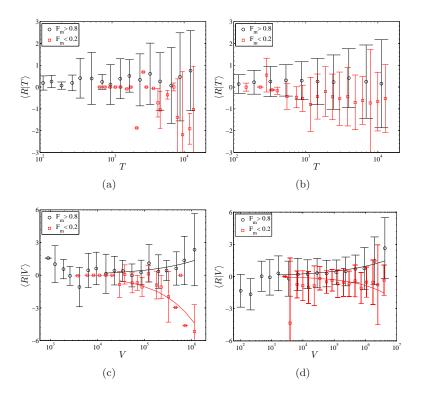


Figure 4. (Color online) Mean conditional scaled price impact of trade packages finished within one day: $\langle R|T\rangle$ for (a) institutions and (b)individuals, and $\langle R|V\rangle$ for (c) institutions and (d) individuals. The solid curves are power-law fits with exponents depicted in Table 3.

differ with the variation of V. Similar to the price-volume relation revealed in many empirical studies, we assume the absolute $\langle R|V\rangle$ for large V follows a power law

$$|\langle R|V\rangle| = AV^{\gamma}.\tag{13}$$

The power-law fits with estimated parameters A and γ listed in Table 3 are illustrated in Figures 4(c) and 4(d). For trade packages with $F_m > 0.8$, γ is about 0.447 for institutions, and 0.295 for individuals. The exponent γ for trade packages with $F_m < 0.2$ is slightly larger. The power-law increase of $\langle R|V \rangle$ at large scales of V may correspond to the purchase or sale of large amounts of shares with the motive to adjust share inventory. However, $\langle R|V \rangle$ for trade packages of institutions with $F_m > 0.8$ does not increase monotonously with the increase of V. The variable $\langle R|V \rangle$ shows a decreasing tendency with increasing V when V is small. This indicates that small trading volumes may also cause large price changes, and it may refer to the purchase or sale of small amounts of shares for the purpose of stock price adjustment.

5.2. Instantaneous price impact of transactions inside trade packages

We have shown the price impact of the entire trade packages, and then we investigate the price impact of individual transactions inside trade packages. Given a transaction *i* inside trade package traded at time t, $p(t_{-})$ is the price before this transaction, and p(t) is the resultant price

Table 3. Estimated parameters for the power-law fit of $\langle R|V\rangle$ for trade packages of both institutions and individuals.

	In	stitution	Ir	ndividual
	A	γ	A	γ
$F_m > 0.8$	0.003	0.447(0.223)	0.016	0.295(0.149)
$F_m < 0.2$	0.001	0.590(0.130)	0.002	0.444(1.290)

immediate after it. The price impact of the transaction i inside trade package is defined as

$$r_i = \ln p(t) - \ln p(t_-), \tag{14}$$

which is the instantaneous change of logarithmic price contributed from the transaction i. To make the price impact comparable over different stocks, the price impact of a particular stock is normalized by its mean absolute value

$$R_i = s_i r_i / \langle |r_i| \rangle, \tag{15}$$

where $s_i = +1$ for buy trades and $s_i = -1$ for sell trades.

5.2.1. $R_i vs t$

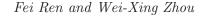
We measure the mean conditional scaled price impact $\langle R_i | t \rangle$ of individual transactions conditioned on the time t. In Figures 5(a) and 5(b), $\langle R_i | t \rangle$ is plotted as a function of the time t for institutions and individuals respectively. The mean conditional scaled price impact of the transactions executed as market orders and limit orders are represented by black circles and red squares in the figure. For market orders, $\langle R_i | t \rangle$ displays a concave U-shaped profile. Though the error bar is quite large, $\langle R_i | t \rangle$ for market orders is mostly positive. For limit orders, $\langle R_i | t \rangle$ is mostly negative, and displays an inverted U-shaped profile. The sign of $\langle R_i | t \rangle$ indicates that the direction of the price change is driven by the market order. In other words, the buyer-initiated trades raise the price, and the seller-initiated trades reduce the price. Moreover, the U-shaped and inverted U-shaped profiles imply that the price impact close to the opening and closing time is larger than the price impact during the remainder of the day. We also investigate the price impact of the transactions concurrently traded with those transactions inside trade packages

$$R_{con} = s_i r_{con} / \langle |r_i| \rangle, \tag{16}$$

where s_i and $\langle |r_i| \rangle$ are the sign and the mean absolute return of transactions inside trade packages, and r_{con} represents the price return caused by the transactions concurrently traded with those transactions inside trade packages. The mean conditional scaled price impact $\langle R_{con}|t\rangle$ (blue diamonds) fluctuates around zero, which indicates that the price impact of market trades is not merely driven by the consecutive trades by large investors.

5.2.2. $R_i vs v$

To investigate the dependence of the price impact of transactions inside trade packages on their trading volumes, we calculate the mean conditional scaled rice impact $\langle R_i | v \rangle$. In Figures 5(c) and 5(d), $\langle R_i | v \rangle$ is plotted for institutions and individuals respectively. One observes that $\langle R_i | v \rangle$ for transactions executed as market orders is mostly positive while that for transactions executed as



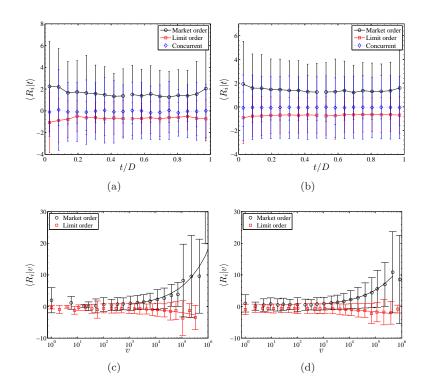


Figure 5. (Color online) Mean conditional scaled price impact of individual transactions inside trade packages finished within one day: $\langle R_i | t \rangle$ for (a) institutions and (b) individuals, and $\langle R_i | v \rangle$ for (c) institutions and (d) individuals. The time t is measured with respect to the time of a day.

limit orders is mostly negative. This further confirms the result that the market order determines the direction of the price change as observed in $\langle R_i | t \rangle$. Similar to $\langle R | V \rangle$ for trade packages, the absolute $\langle R_i | v \rangle$ of transactions inside trade packages follows a power law

$$|\langle R_i | v \rangle| = B v^k, \tag{17}$$

when v is large enough $v > 10^3$. The estimated parameters B and k for the power-law fit of $\langle R_i | v \rangle$ are listed in Table 4. The exponent k for transactions executed as market orders is larger than that for transactions executed as limit orders, which indicates that for the isolated transactions inside trade packages the price impact is remarkably affected by the market order. However, the cumulative impact of trade packages with small fraction of market orders is comparable with the cumulative impact of trade packages with large fraction of market orders. In fact, the exponent γ of $\langle R | V \rangle$ for packages with $F_m < 0.2$ is slightly larger than that for packages with $F_m > 0.8$. This may because the investors use different strategies for the accomplishment of trade packages. Like a sequence of mostly buyer-initiated trades, a sequence of sales mostly executed as limit orders can also raise the price, affected by the buyer-initiated trades on the opposite sides.

Table 4. Estimated parameters for the power-law fits of $\langle R_i | v \rangle$ for transactions inside trade packages of both institutions and individuals.

	In	stitution	In	dividual
	В	k	B	k
market order	0.04	0.45(0.11)	0.05	0.40(0.02)
limit order	0.09	0.27(0.12)	0.15	0.21(0.05)

5.3. Temporary price impact of transactions inside trade packages

5.3.1. Impact of trading volumes on current and following price returns

Numerous studies have focused on the influence of trading volumes or volume imbalances on price returns (Wood *et al.* 1985, Karpoff 1987, Gallant *et al.* 1992, Saatcioglu and Starks 1998, Lillo *et al.* 2003, Plerou *et al.* 2002, Chordia and Subrahmanyam 2004). We analyze the temporary impact of transactions inside trade packages in relation to their trading volumes. Suppose $r(t) = \ln p(t) - \ln p(t-1)$ is the price return at time t, v(t) is the trading volume of a transaction inside trade package traded at time t. The returns of a certain stock are normalized by its standard deviation. To explain the influence of the trading volume at time t on the price return at later time t + i, we estimate a regression of the following form

$$R(t+i) = \beta_0^* + \beta_i s \ln v(t) + \epsilon(t), \qquad (18)$$

where s is the sign of the transaction. We measure the impact of the trading volumes v(t) within trade package on the current price return i = 0 and the following price returns i = 5, 10, 15, 20, 25seconds. It has been empirically verified that the price return has a power-law dependence on the trading volume (Hasbrouck 1991, Plerou *et al.* 2002, Chordia and Subrahmanyam 2004, Zhou 2011), also confirmed in the measure of $\langle R_i | v \rangle$. The first-order approximation of the logarithmic return is assumed, and a linear regression of the return against logarithmic trading volume is used to approximate their power-law relations.

Table 5 reports the estimated coefficients of regressions using the records of transactions inside trade packages executed as market orders from institutions. Positive coefficient β_{0sec} is observed in all the 23 stocks, which further confirms the finding that the sign of price return is determined by the sign of the market order as revealed in the measure of $\langle R_i | t \rangle$. The relevant t-statistics are also depicted in Table 5. The impact of trading volume on the current price return is significant for most of stocks except for stocks 000009,000012,000429,000550. This indicates that the instantaneous impact of the trading volumes executed as market orders is positive and significant. We find the price tends to reverse soon after the transaction inside trade package, showing negative β_i with i > 0. This reminds us of the significant price reversal after large price changes (Zawadowski et al. 2004, Mu et al. 2010). The magnitudes of β_i with i > 0 are significantly smaller than β_{0sec} , and decrease with the increase of time lag *i*. Coefficient β_{5sec} is negative and significant for more than half of the stocks, and negative and significant β_{10sec} is also observed in almost half of the stocks. This implies that for almost half of the stocks the trading volumes of transactions inside trade packages have temporary negative effects on price returns for at least 5-10 seconds. With rare exceptions, the stocks have nonsignificant coefficients β_i for large time lag $i \ge 15$ seconds. For the trading volumes of transactions inside trade packages executed as limit orders, a temporary impact is also observed. Negative β_{0sec}

Fei Ren and Wei-Xing Zhou

Table 5. Coefficients and t-statistics for the linear fit of Equation (18) using the records of transactions inside trade packages executed as market orders from institutions. Coefficients marked with * are statistically significant at 5% level.

Code	β_0	<i>t</i> -stat	β_5	<i>t</i> -stat	β_{10}	<i>t</i> -stat	β_{15}	<i>t</i> -stat	β_{20}	<i>t</i> -stat	β_{25}	<i>t</i> -stat
000001	0.062^{*}	6.91	-0.026^{*}	-3.67	-0.008	-1.17	0.000	0.05	0.000	0.12	0.002	0.26
000002	0.094^{*}	24.02	-0.034^{*}	-11.58	-0.014^{*}	-4.38	-0.009^{*}	-3.09	0.004	1.34	0.005	1.77
000009	0.242	1.23	-0.545	-1.74	0.277	1.86	-0.334	-1.17	-0.053	-0.23	-0.157	-0.83
000012	0.077	1.43	0.023	0.80			-0.020	-1.28	0.035	1.05	-0.017	-0.75
000016	0.134^{*}	13.01	-0.013^{*}	-2.59	-0.007	-1.48	-0.019^{*}	-2.72	-0.007	-0.19	-0.009	-1.43
000021	0.132^{*}	8.39	-0.005	-0.46	-0.009	-0.88	-0.012	-1.06	0.002	0.19	-0.008	-0.74
000024	0.131^{*}	14.90	-0.020^{*}	-3.62	-0.011^{*}	-2.20	-0.002	-0.70	-0.009^{*}	-2.09	0.003	0.56
000027	0.073^{*}	5.48	-0.022^{*}	-2.32	0.012	1.29	-0.007	-0.77	0.001	0.16	0.022^{*}	2.10
000063	0.119^{*}	15.51	-0.009	-1.88	-0.008*	-2.11	-0.003	-0.63	-0.002	-0.64	-0.001	-0.21
000066	0.136^{*}	6.09	-0.018^{*}	-2.98	0.003	0.57	-0.011	-0.96	-0.006	-0.71	0.003	0.40
000088	0.125^{*}	26.45	-0.003	-1.50	-0.007^{*}	-4.16	-0.008^{*}	-4.39	-0.004	-1.58	0.002	1.45
000089	0.100^{*}	22.83	-0.030^{*}	-8.37	-0.009^{*}	-3.30	-0.002	-0.76	0.003	1.27	0.002	1.00
000406	0.105^{*}	6.15	-0.015	-1.87	-0.022	-1.73	-0.008	-0.89	0.020	1.60	-0.006	-0.73
000429	0.105	0.64	-0.282	-0.86	-0.105	-0.64					0.166	0.65
000488	0.128^{*}	31.92	-0.026^{*}	-11.70	-0.015^{*}	-6.66	-0.003	-1.60	-0.005	-1.95	-0.003	-1.60
000539	0.107^{*}	14.42	-0.031^{*}	-6.30	-0.004	-0.91	-0.001	-0.17	-0.005	-1.19	-0.003	-0.64
00054	0.139^{*}	3.63	-0.013	-0.78	-0.014	-1.22	-0.016	-0.54	0.011	1.37	0.023	1.10
000550	1.403	2.39										
000581	0.115^{*}	21.53	-0.010^{*}	-3.63	-0.008^{*}	-3.19	-0.005	-1.90	-0.005^{*}	-2.28	-0.005^{*}	-1.98
000625	0.085^{*}	18.60	-0.025^{*}	-6.91	-0.021^{*}	-5.15	-0.004	-1.13	-0.004	-1.04	0.000	-0.07
000709	0.098^{*}	11.60	-0.031^{*}	-5.35	-0.013	-1.89	-0.006	-1.18	-0.014^{*}	-2.46	0.002	0.28
000720	0.162^{*}	13.47	-0.015^{*}	-2.04	0.009^{*}	1.99	-0.008	-1.02	0.003	0.48	0.003	0.46
000778	0.130^{*}	5.06	-0.015	-1.52	-0.010	-1.43	-0.004	-0.62	-0.013	-1.07	-0.005	-0.63

is obtained for most of the stocks, indicating the price return has a sign opposite to that of the trading volume. Positive β_{5sec} and β_{10sec} further confirm the price reversal soon after the transaction inside trade package.

The temporary impact of transactions inside trade packages for individuals persists over a horizon longer than the impact time for institutions. In Table 6, the estimated coefficients β_i with i = 0, 5, 10, 15, 20, 25 seconds using the records of transactions inside trade packages executed as market orders from individuals are depicted. Coefficient β_{0sec} is positive and significant for all the 23 stocks, which further verifies the strong impact of the trading volume on the current price return. Moreover, β_{0sec} is larger than the magnitudes of coefficients β_i with i > 0. Coefficients β_i with time lag $5 \le i \le 20$ seconds are negative and significant for most stocks, and β_{25sec} is significant for almost half of the stocks. This implies that the trading volumes of transactions inside trade packages for individuals have temporary negative effects on price returns for about 20-25 seconds. Similar to the trading volumes executed as limited orders from institutions, the trading volumes executed as limited orders from individuals have a negative impact on current price returns, and the following price returns tend to reverse soon.

5.3.2. Modeling price returns

It has been shown that the trading volumes of transactions inside trade packages have a significant impact on price returns. We model the price return R(t) taking into account both the autoregressive components of previous returns R(t-j) and the previous trading volumes v(t-i) within trade packages. The regression from is

$$R(t) = \beta_0^* + \sum_{j=5}^J \gamma_j R(t-j) + \sum_{i=0}^I \beta_i s \ln v(t-i) + \epsilon(t),$$
(19)

Ia				statistics f ecuted as i stat	market o		n individ	luals. Coef	0			
odo	ße	tetot	ß-	tetat	Bro	tetat	B	tetat	Baa	tetat	Bar	tat

Code	β_0	t-stat	β_5	t-stat	β_{10}	<i>t</i> -stat	β_{15}	t-stat	β_{20}	t-stat	β_{25}	<i>t</i> -stat
000001	0.090^{*}	104.65	-0.042^{*}	-53.52	-0.011^{*}	-14.14	-0.003^{*}	-3.91	-0.001	-0.83	-0.003^{*}	-3.52
000002	0.084^{*}	91.13	-0.030^{*}	-40.15	-0.009^{*}	-11.54	-0.004^{*}	-4.77	-0.001	-1.81	0.000	0.43
000009	0.096^{*}	67.99	-0.032^{*}	-29.81	-0.010^{*}	-8.61	-0.007^{*}	-5.40	-0.003^{*}	-2.83	-0.001	-0.87
000012	0.085^{*}	91.55	-0.026^{*}	-36.16	-0.013^{*}	-17.23	-0.007^{*}	-9.83	-0.003^{*}	-4.72	0.011^{*}	14.90
000016	0.110^{*}	58.77	-0.020^{*}	-19.54	-0.014^{*}	-12.00	-0.005^{*}	-4.70	-0.004^{*}	-4.02	0.000	-0.26
000021	0.110^{*}	74.10	-0.029^{*}	-27.54	-0.011^{*}	-10.63	-0.006^{*}	-5.82	-0.003^{*}	-3.05	-0.002	-1.47
000024	0.112^{*}	50.20	-0.015^{*}	-12.02	-0.011^{*}	-8.12	-0.009^{*}	-6.83	-0.003^{*}	-1.97	-0.004^{*}	-3.09
000027	0.099^{*}	90.69	-0.026^{*}	-31.90	-0.012^{*}	-15.75	-0.005^{*}	-6.32	-0.003^{*}	-3.94	0.002^{*}	2.83
000063	0.058^{*}	62.64	-0.014^{*}	-17.99	-0.004^{*}	-9.63	-0.003^{*}	-3.80	-0.001	0.71	0.000	0.39
000066	0.111^{*}	53.63	-0.028^{*}	-21.86	-0.013^{*}	-5.54	-0.008^{*}	-6.22	-0.006^{*}	-4.33	-0.004^{*}	-2.95
000088	0.122^{*}	51.29	-0.008^{*}	-8.51	-0.005^{*}	-10.35	-0.004^{*}	-4.09	-0.004^{*}	-3.92	0.001	0.71
000089	0.107^{*}	75.79	-0.016^{*}	-18.33	-0.009^{*}	-13.92	-0.005^{*}	-5.75	-0.003^{*}	-3.26	0.002^{*}	2.03
000406	0.111^{*}	75.14	-0.030^{*}	-28.31	-0.015^{*}	-7.39	-0.009^{*}	-8.87	-0.003^{*}	-3.03	0.000	-0.18
000429	0.094^{*}	47.67	-0.023^{*}	-18.50	-0.010^{*}	-20.51	-0.006^{*}	-4.59	-0.003^{*}	-1.99	-0.003^{*}	-2.64
000488	0.126^{*}	107.67	-0.022^{*}	-36.86	-0.013^{*}	-12.49	-0.006^{*}	-10.51	-0.003^{*}	-5.20	-0.002^{*}	-2.66
000539	0.102^{*}	75.63	-0.022^{*}	-25.49	-0.011^{*}	-5.05	-0.004^{*}	-4.53	-0.004^{*}	-4.73	-0.003^{*}	-3.47
000541	0.130^{*}	50.71	-0.011^{*}	-9.72	-0.006^{*}	-12.55	-0.005^{*}	-4.70	-0.003^{*}	-2.61	-0.002	-1.91
000550	1.107^{*}	87.79	-0.026^{*}	-28.81	-0.011^{*}	-8.81	-0.008*	-9.20	0.001	1.57	-0.001	-0.79
000581	0.126^{*}	62.91	-0.012^{*}	-12.50	-0.009^{*}	-3.19	-0.008*	-7.76	-0.003^{*}	-3.49	-0.003^{*}	-2.82
000625	0.092^{*}	92.89	-0.028^{*}	-36.80	-0.012^{*}	-16.37	-0.006^{*}	-7.97	-0.001	-1.94	-0.002^{*}	-3.02
000709	0.096^{*}	64.89	-0.020^{*}	-20.59	-0.015^{*}	-13.10	-0.008^{*}	-8.90	-0.004^{*}	-3.85	0.001	0.87
000720	0.150^{*}	89.91	-0.012^{*}	-12.02	-0.005^{*}	-5.07	-0.002^{*}	-2.13	0.001	0.95	0.002	1.55
000778	0.105^{*}	63.38	-0.020^{*}	-17.23	-0.006^{*}	-6.30	-0.005^{*}	-5.47	-0.003^{*}	-3.75	0.000	0.31

where $\ln v(t-i) = 0$ when there is no transaction inside trade package executed at time t-i. We do not separately consider the effects of trading volumes of the transactions concurrently traded with those transactions inside trade packages, but contribute their impact to the corresponding price returns. The coefficient β_i reflects the response of the return R(t) to the trading volume of transaction inside trade package executed *i* seconds before time *t*. We have verified that the trading volumes of transactions inside trade packages have a temporary impact on price returns for less than half a minute, and therefore we restrict I = 25 seconds. The parameter J is also set to J = 25 seconds to simplify the regression.

We report the estimated coefficients β_i by fitting Equation (19) with i = 0, 5, 10, 15, 20, 25seconds using the records of transactions inside trade packages executed as market orders from institutions in Table 7. According to the R^2 in the last column, the fitted model could explain considerable portion, generally has $R^2 \geq 20\%$, of the variance in price returns. For i = 0, positive and significant coefficient β_{0sec} is observed in all the 23 stocks, displaying values significantly larger than the magnitudes of β_i with i > 0. This further confirms that the trading volumes of transactions inside trade packages executed as market orders have a strong impact on current price returns. However, the negative relation between the price return and the trading volume executed 5 seconds before is weakened, not as significant as that observed in the simple regression of Equation (18). After taking into account the autoregressive components, only five stocks have significant coefficients β_{5sec} , and four of them are negative. To further increase the time lag i, the number of stocks which have significant coefficients β_i is even smaller. The shortening of the impact time may because the price return can be partially explained by the autoregressive components of previous returns.

We also obtain the coefficients β_i by estimating Equation (19) using the records of transactions inside trade packages executed as market orders from individuals as depicted in Table 8. The R^2 for individuals is generally smaller than that for institutions, but still has values $\geq 10\%$ for

Table 7. Coefficients and t-statistics for the linear fit of Equation (19) with I = 25 and J = 25 seconds using the records of transactions inside trade packages executed as market orders from institutions. Coefficients marked with * are statistically significant at 5% level.

Fei Ren and Wei-Xing Zhou

								0					
Code	β_0	t-stat	β_5	t-stat	β_{10}	t-stat	β_{15}	t-stat	β_{20}	<i>t</i> -stat	β_{25}	t-stat	R^2
000001	0.075^{*}	11.63	0.007	0.96	-0.020^{*}	-2.87	-0.013	-1.89	-0.012	-1.66	0.007	1.04	0.23
000002	0.085^{*}	31.28	-0.007^{*}	-2.43	-0.008*	-2.54	-0.006^{*}	-2.05	-0.001	-0.48	-0.005	-1.62	0.24
000009	0.027	0.74	-0.041	-1.18	-0.045	-1.17	-0.048	-1.21	-0.016	-0.41	-0.027	-0.62	0.17
000012	0.103^{*}	3.76	0.023	0.72	0.016	0.52	-0.010	-0.32	0.007	0.23	-0.002	-0.06	0.27
000016	0.135^{*}	20.11	0.002	-0.25	-0.008	-1.01	0.001	0.15	-0.012	-1.40	-0.008	-0.94	0.29
000021	0.137^{*}	11.80	0.023	1.64	-0.013	-0.88	-0.011	-0.81	-0.003	-0.25	-0.010	-0.71	0.29
000024	0.129^{*}	24.81	0.000	0.06	-0.010	-1.57	-0.005	-0.80	-0.002	-0.33	-0.005	-0.69	0.30
000027	0.082^{*}	9.28	0.011	1.10	-0.001	-0.07	0.001	0.12	0.007	0.68	0.013	1.27	0.20
000063	0.106^{*}	25.72	0.005	0.92	0.003	0.56	0.005	0.96	0.003	0.60	-0.004	-0.75	0.27
000066	0.154^{*}	15.03	0.002	0.16	-0.015	-1.18	-0.007	-0.56	-0.005	-0.35	-0.021	-1.59	0.31
000088	0.064^{*}	37.48	-0.007^{*}	-3.62	-0.001	-1.05	0.000	0.09	0.000	-0.17	0.003	1.25	0.13
000089	0.093^{*}	35.43	0.005	1.83	0.000	-1.54	0.002	0.60	0.002	0.80	-0.002	-0.77	0.29
000406	0.107^{*}	9.87	-0.001	-0.10	-0.014	1.16	0.006	0.49	0.000	-0.04	0.000	0.02	0.17
000429	0.002	0.02	-0.103	-1.28	-0.084	-0.64	-0.035	-0.43	-0.040	-0.50	-0.048	-0.60	0.18
000488	0.128^{*}	54.40	-0.004	-1.66	-0.004	-0.82	-0.002	-0.81	-0.003	-1.22	-0.004^{*}	-3.15	0.23
000539	0.093^{*}	23.32	-0.013^{*}	-2.83	0.005	-0.02	-0.005	-1.16	-0.001	-0.30	0.000	-0.02	0.23
000541	0.161^{*}	8.18	-0.015	-0.59	-0.016	-3.28	-0.005	-0.20	0.022	0.88	-0.003	-0.10	0.34
000550	0.137	1.92	-0.085	-0.76	-0.087	-0.86	-0.087	-0.83	-0.088	-0.82	-0.085	-1.15	0.80
000581	0.084^{*}	37.77	-0.007^{*}	-2.63	0.000	3.97	-0.013^{*}	-4.96	-0.008^{*}	-2.87	-0.004	-1.32	0.19
000625	0.075^{*}	22.70	-0.004	-1.24	-0.012^{*}	-0.90	-0.005	-1.43	-0.005	-1.38	-0.007	-1.80	0.20
000709	0.084^{*}	16.25	-0.011	-1.84	-0.005	-1.89	-0.013^{*}	-2.12	-0.015^{*}	-2.37	-0.002	-0.23	0.26
000720	0.122^{*}	20.49	0.021^{*}	3.05	0.027^{*}	1.99	0.008	1.19	0.017^{*}	0.50	0.011	1.52	0.24
000778	0.134^{*}	11.89	-0.003	0.20	-0.012	-1.43	-0.014	-1.04	-0.010	-0.74	-0.007	-0.52	0.32

most stocks. Coefficient β_{0sec} for individuals is positive and significant for all the stocks, but approximately one order of magnitude smaller than β_{0sec} for institutions. This implies that the positive impact of trading volumes on current price returns for individuals is not as strong as that for institutions. More than half of the stocks have negative and significant coefficients β_i for $i \leq 25$ seconds. This indicates that for more than half of the stocks the trading volumes of transactions inside trade packages have a temporary negative impact for at least 25 seconds. In comparison with the trading volumes for institutions, the trading volumes for individuals have a negative price impact over a relatively longer horizon even after considering the autoregressive components of previous returns.

6. Summary

This paper studies the characteristic properties of trade packages made by both institutional and individual investors trading on Shenzhen Stock Exchange. The sequence of transactions are grouped into packages with mostly buy or sell trades separated by the break of 1, 5, 10 days. The probability distributions of the variables, i.e., the execution time T, the number of trades N and the total trading volume V, characterizing trade packages show power-law tails, and a power-law fitting method based on KS statistic is adopted to estimate their exponents. The exponent of the execution time is smaller than 1.0, and the exponent of the trades number is around 3.0 close to that of the total trading volume. The exponents vary with the break length, and tend to be constant for the break length longer than 5 days. Moreover, the exponents for individuals are slightly larger than those for institutions. The scaling relations between these variables are also detected. All the scaling exponents show values smaller than 1.0, different from those found by Vaglica *et al.* (2008) and Moro *et al.* (2009).

We have also studied the trading profile of the trade packages accomplished within one day. By investigating the mean trading volume of the individual transactions inside trade packages, we find that large amounts of shares are more likely to be executed close to the opening and closing 1:9

Table 8. Coefficients and t-statistics for the linear fit of Equation (19) with $I = 25$ and $J = 25$ s	econds
using the records of transactions inside trade packages executed as market orders from individ	uals.
Coefficients marked with $*$ are statistically significant at 5% level.	

Code	β_0	t-stat	β_5	t-stat	β_{10}	t-stat	β_{15}	t-stat	β_{20}	t-stat	β_{25}	t-stat	R^2
000001	0.008^{*}	65.42	-0.002^{*}	-11.77	-0.001*	-8.69	-0.001^{*}	-6.01	-0.002^{*}	-14.38	-0.001^{*}	-5.37	0.19
000002	0.012^{*}	58.75	-0.006^{*}	-25.44	0.000	1.64	0.001^{*}	2.04	-0.001^{*}	-3.09	0.000	-0.67	0.15
000009	0.015^{*}	55.03	-0.004^{*}	-10.95	0.001^{*}	2.64	0.000	1.14	-0.002^{*}	-7.02	-0.002^{*}	-5.87	0.14
000012	0.044^{*}	108.68	-0.008*	-19.14	-0.003^{*}	-6.01	-0.003^{*}	-7.61	-0.002^{*}	-4.30	-0.003^{*}	-6.01	0.20
000016	0.079^{*}	85.62	-0.004^{*}	-3.56	-0.005^{*}	-4.69	-0.002^{*}	-2.31	-0.005^{*}	-5.54	-0.006^{*}	-6.03	0.19
000021	0.012^{*}	48.69	-0.003^{*}	-10.68	0.000	-1.03	0.000	1.48	-0.002^{*}	-6.97	-0.004^{*}	-14.15	0.11
000024	0.021^{*}	35.31	-0.008*	-11.68	-0.003^{*}	-4.00	0.002^{*}	3.30	0.002^{*}	2.42	-0.002^{*}	-3.09	0.09
000027	0.007^{*}	50.89	-0.004^{*}	-26.08	0.002^{*}	13.20	-0.002^{*}	-14.16	0.000^{*}	-2.31	0.000^{*}	-2.64	0.11
000063	0.009^{*}	62.02	-0.003^{*}	-19.95	-0.001*	-7.09	0.000^{*}	-2.08	0.000^{*}	1.98	-0.001^{*}	-6.86	0.17
000066	0.042^{*}	55.68	-0.008^{*}	-9.32	-0.004^{*}	-4.33	-0.003^{*}	-3.28	-0.004^{*}	-5.09	-0.001	-1.60	0.14
000088	0.003^{*}	26.57	-0.002^{*}	-11.87	0.000	0.26	0.000	0.22	0.000	-1.86	-0.001^{*}	-6.70	0.03
000089	0.012^{*}	54.11	-0.001^{*}	-2.27	0.001^{*}	2.69	0.000	-0.05	0.001^{*}	4.00	0.001^{*}	2.14	0.09
000406	0.027^{*}	61.79	-0.006^{*}	-11.87	-0.002^{*}	-3.429	-0.002^{*}	-5.13	0.000	0.33	-0.001	-1.14	0.15
000429	0.074^{*}	73.05	-0.007^{*}	-5.42	-0.003^{*}	-2.59	-0.005^{*}	-4.33	-0.007^{*}	-5.83	-0.007^{*}	-5.51	0.18
000488	0.127^{*}	208.16	-0.006^{*}	-8.84	-0.005^{*}	-7.06	0.000	-0.35	-0.003^{*}	-3.93	-0.005^{*}	-7.69	0.25
000539	0.005^{*}	106.43	-0.002^{*}	-30.85	0.001^{*}	8.60	-0.001^{*}	-10.32	0.000^{*}	-5.03	0.000^{*}	-6.55	0.14
000541	0.105^{*}	81.61	-0.006^{*}	-4.31	-0.009^{*}	-5.60	-0.013^{*}	-8.14	-0.008^{*}	-5.10	-0.007^{*}	-4.50	0.19
000550	0.005^{*}	51.66	-0.002^{*}	-15.97	-0.001^{*}	-4.99	0.000	0.71	0.000	1.33	-0.001^{*}	-4.10	0.09
000581	0.005^{*}	32.87	-0.003^{*}	-17.42	0.001^{*}	2.64	-0.001^{*}	-3.68	0.000	1.29	-0.001^{*}	-6.79	0.05
000625	0.006^{*}	60.96	-0.001^{*}	-9.98	0.000	1.50	0.001	0.50	0.000	-0.27	0.000^{*}	-3.25	0.14
000709	0.008^{*}	48.83	-0.002^{*}	-8.36	0.000	-1.49	-0.002^{*}	-9.89	0.001^{*}	2.57	0.000	-0.90	0.15
000720	0.019^{*}	76.99	-0.002^{*}	-6.94	0.001	1.98	-0.001^{*}	-4.89	0.001^{*}	5.08	0.000	-1.54	0.08
000778	0.055^{*}	77.13	0.000	-0.29	0.001	0.86	-0.002	-1.92	-0.003^{*}	-4.54	0.001	0.84	0.17

time respectively for institutions and individuals. The probability distribution of the transaction time shows that both institutional and individual investors trade more frequently after the midday break, and it displays a maximum at the closing time of the day. This phenomena might be explained by their preferences on the initial and final time of trade packages. The profile of the total trading volume further implies that institutions may be more informed than individuals.

The price impact of trade packages and its relations with the execution time T and the total trading volume V are analyzed respectively. We find the price impact remains nonzero over the whole period of execution time. The price impact has an empirical power-law relation with the total trading volume. Furthermore, the instantaneous price impact of the transactions inside trade packages is investigated, and transactions close to the opening and closing time of the day have a stronger impact than those during the remainder of the day. Similar to trade packages, the transactions inside trade packages also show a power-law dependence on their corresponding volumes. To study the temporary impact of transactions inside trade packages, we regress the price return against its current and previous trading volumes within trade packages, and further model the price return taking into account both the autoregressive components of previous returns and the current and previous trading volumes within trade packages. The regression results show that the trading volumes of the transactions inside trade packages have a strong positive impact on current price returns, while the reversals of the following prices are less strong and persist over only a few seconds. This may help explain the permanent impact of isolated transactions revealed in the empirical study of block trades (Keim and Madhavan 1996, Gregoriou 2008, Kraus and Stoll 1972, Gemmill 1996). In addition, the impact of trading volumes on current price returns for institutions is stronger than that for individuals, and the price reversal for individuals persists over a horizon relatively longer than that for institutions. Though the transactions inside trade packages have a temporary impact persisting over only a few seconds, the cumulative impact of trade packages is significant over the whole period of execution time (Gemmill 1996).

22

Acknowledgements

We are grateful to Zhi-qiang Jiang (School of Business, East China University of Science and Technology) for preprocessing the data analyzed in this work. This work was partially supported by the National Natural Science Foundation (No. 10905023), the Zhejiang Provincial Natural Science Foundation of China (No. Z6090130), Humanities and Social Sciences Fund sponsored by Ministry of Education of the People's Republic of China (No. 09YJCZH042), and the Fundamental Research Funds for the Central Universities.

REFERENCES

References

- Aitken, M. and Frino, A., Execution costs associated with institutional trades on the Australian Stock Exchange. *Pacific-Basin Financ. J.*, 1996, 4, 45–58.
- Alfonsi, A., Fruth, A. and Schied, A., Optimal execution strategies in limit order books with general shape functions. *Quant. Financ.*, 2010, 10, 143–157.
- Almgren, R.F., Optimal execution with nonlinear impact functions and trading-enhanced risk. Appl. Math. Financ., 2003, 10, 1–18.
- Chan, K. and Fong, W.M., Trade size, order imbalance, and the volatility-volume relation. J. Financ. Econ., 2000, 57, 247–273.
- Chan, K.C. and Lakonishok, J., The behavior of stock prices around institutional trades. J. Financ., 1995, 50, 1147–1174.
- Chiyachantana, C.N., Jain, P.K., Jiang, C. and Wood, R.A., International evidence on institutional trading behavior and price impact. J. Financ., 2004, 59, 869–898.
- Chordia, T. and Subrahmanyam, A., Order imbalance and individual stock returns: Theory and evidence. J. Financ. Econ., 2004, 72, 485–518.
- Clauset, A., Shalizi, C.R. and Newman, M.E.J., Power-law distributions in empirical data. SIAM Rev., 2009, 51, 661–703.
- Farmer, J.D., Gerig, A., Lillo, F. and Waelbroeck, H., How efficiency shapes market impact [online]., 2011. (accessed http://arxiv.org/abs/1102.5457v1).
- Gallagher, D.R. and Looi, A., Trading behaviour and the performance of daily institutional trades. Ann. Financ., 2006, 46, 125–147.
- Gallant, A.R., Rossi, P.E. and Tauchen, G., Stock prices and volume. Rev. Financ. Stud., 1992, 5, 199–242.
- Gemmill, G., Transparency and liquidity: A study of block trades in the London Stock Exchange under different publication rules. J. Financ., 1996, **51**, 1765–1790.
- Giambona, E. and Golec, J., Strategic trading in the wrong direction by a large institutional insider. J. Emp. Financ., 2010, 17, 1–22.
- Gregoriou, A., The asymmetry of the price impact of block trades and the bid-ask spread Evidence from the London Stock Exchange. J. Econ. Surveys, 2008, **35**, 191–199.
- Hasbrouck, J., Measuring the information content of stock trades. J. Financ., 1991, 46, 179–207.
- Jain, P.K., Discussion of Equity trading by institutional investors: Evidence on order submission strategies by Naes and Skjeltorp. J. Behav. Financ., 2003, 27, 1819–1821.
- Karpoff, J.M., The relation between price changes and trading volume: A survey. J. Financ. Quant. Anal., 1987, 22, 109–126.
- Keim, D.B. and Madhavan, A., Anatomy of the trading process: Empirical evidence on the behavior of institutional traders. J. Financ. Econ., 1995, **37**, 371–398.
- Keim, D.B. and Madhavan, A., The upstairs market for large-block transactions: analysis and measurement of price effects. *Rev. Financ. Stud.*, 1996, 9, 1–36.

- Kraus, A. and Stoll, H.R., Price impact of block trading on the new york stock exchange. J. Financ., 1972, 27, 569–588.
- Lillo, F., Farmer, J.D. and Mantegna, R., Master curve for price impact function. Nature, 2003, 421, 129–130.
- Lim, M. and Coggins, R., The immediate price impact of trades on the Australian Stock Exchange. Quant. Financ., 2005, 5, 365–377.
- Moro, E., Vicente, J., Moyano, L.G., Gerig, A., Farmer, J.D., Vaglica, G. and Lillo, F., Market impact and trading profile of hidden orders in stock markets. *Phys. Rev. E*, 2009, **80**, 066102.
- Mu, G.H., Zhou, W.X., Chen, W. and Kertész, J., Order flow dynamics around extreme price changes on an emerging stock market. *New J. Phys.*, 2010, **12**, in press.
- Næs, R. and Skjeltorp, J.A., Order book characteristics and the volume-volatility relation: Empirical evidence from a limit order market. J. Financ. Markets, 2006, 9, 408–432.
- Obizhaeva, A. and Wang, J., Optimal trading strategy and supply/demand dynamics [online]. , 2010. (accessed http://ssrn.com/abstract=686168).
- Plerou, V., Gopikrishnan, P., Gabaix, X. and Stanley, H.E., Quantifying stock-price response to demand fluctuations. *Phys. Rev. E*, 2002, 66, 027104.
- Prino, A., Jarnecic, E. and Lepone, A., The determinants of the price impact of block trades: Further evidence. *ABACUS*, 2007, **43**, 94–106.
- Saar, G., Price impact asymmetry of block trades: An institutional trading explanation. Rev. Financ. Stud., 2001, 14, 1153–1181.
- Saatcioglu, K. and Starks, L.T., The stock price-volume relationship in emerging stock markets: The case of Latin America. *Int. J. Forecast.*, 1998, **14**, 215–225.
- Vaglica, G., Lillo, F. and Mantegna, R.N., Statistical identification with hidden Markov models of large order splitting strategies in an equity market. New J. Phys., 2010, 12, 075031.
- Vaglica, G., Lillo, F., Moro, E. and Mantegna, R.N., Scaling laws of strategic behavior and size heterogeneity in agent dynamics. *Phys. Rev. E*, 2008, 77, 036110.
- Wood, R.A., McInish, T.H. and Ord, J.K., An investigation of transactions data for NYSE stocks. J. Financ., 1985, 40, 723–739.
- Ying, C.C., Stock market prices and volumes of sales. *Econometrica*, 1966, **34**, 676–685.
- Zawadowski, A.G., Kertész, J. and Ador, G., Large price changes on small scales. *Physica A*, 2004, **344**, 221–226.
- Zhou, W.X., Universal price impact functions of individual trades in an order-driven market [online]. , 2011. (accessed http://arxiv.org/abs/0708.3198v2).
- Zhou, W.X. and Sornette, D., Antibubble and prediction of China's stock market and real-estate. *Physica A*, 2004, **337**, 243–268.