# Quintessence-momentum as link between mass and charge 

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#### Abstract

The natural constants, $G, h, e, \mu_{0}$ and $m_{e}$ are presented as geometrical shapes in terms of Planck momentum, $\alpha$ (Sommerfeld fine structure constant) and $c$. A square root solution of Planck momentum denoted Quintessence-momentum $Q$ links the mass and charge constants. The electron formula describes a dimensionless magnetic monopole. The Rydberg constant $R_{\infty}$, the most accurate of the natural constants, is used for crossreference, the solutions are consistent with CODATA 2010 precision.


## 1 Introduction

Some things never change. Physicists call them the constants of nature. Such quantities as the velocity of light, c, Newton's constant of gravitation, G, and the mass of the electron, me, are assumed to be the same at all places and times in the universe. They form the scaffolding around which the theories of physics are erected, and they define the fabric of our universe. Physics has progressed by making ever more accurate measurements of their values. And yet, remarkably, no one has ever successfully predicted or explained any of the constants. Physicists have no idea why they take the special numerical values that they do. In SI units, c is 299,792,458; G is $6.673 \mathrm{e}-11$; and me is $9.10938188 \mathrm{e}-31$-numbers that follow no discernible pattern. The only thread running through the values is that if many of them were even slightly different, complex atomic structures such as living beings would not be possible. The desire to explain the constants has been one of the driving forces behind efforts to develop a complete unified description of nature, or "theory of everything." Physicists have hoped that such a theory would show that each of the constants of nature could have only one logically possible value. It would reveal an underlying order to the seeming arbitrariness of nature. [1]

Formulas are proposed for the natural constants $G, h, e$ (or $\left.\mu_{0}\right)$ and $m_{e}$, as derivatives of the square root of Planck momentum (denoted $Q$ ), $c$ and $\alpha$. The electron is formed from dimensionless magnetic monopoles. The formulas and units are cross referenced with each other to confirm continuity and the numerical solutions, including the Rydberg constant, are consistent with CODATA 2010 precision.

Quintessence momentum $Q$ is proposed as a square root solution to Planck momentum, whereby;

$$
\begin{gathered}
Q=1.01911341 \ldots \text { units }=\sqrt{\frac{\mathrm{kg} \cdot \mathrm{~m}}{\mathrm{~s}}} \\
\text { Planck momentum }=2 . \pi \cdot Q^{2}, \text { units }=\frac{\mathrm{kg} \cdot \mathrm{~m}}{\mathrm{~s}}
\end{gathered}
$$

## 2 General formulas

If we assign to the Ampere;

$$
\begin{equation*}
A=\frac{8 \cdot c^{3}}{\pi \cdot \alpha \cdot Q^{3}}, \text { units }=\frac{m^{2}}{\mathrm{~kg} \cdot \mathrm{~s}^{2} \cdot \sqrt{(\mathrm{~kg} \cdot \mathrm{~m} / \mathrm{s})}} \tag{1}
\end{equation*}
$$

then by replacing the SI units for the natural constants with $2 . \pi . Q=k g . \mathrm{m} / \mathrm{s}, l_{p}=m$ and $c=m / s ;$

$$
\begin{gather*}
m_{P}=\frac{2 \cdot \pi \cdot Q^{2}}{c}, \text { units }=\mathrm{kg}  \tag{2}\\
G=\frac{l_{p} \cdot c^{3}}{2 \cdot \pi \cdot Q^{2}}, \text { units }=\frac{\mathrm{m}^{3}}{\mathrm{~kg} \cdot \mathrm{~s}^{2}}  \tag{3}\\
h=2 \cdot \pi \cdot Q^{2} \cdot 2 \cdot \pi \cdot l_{p}, \text { units }=\frac{\mathrm{kg} \cdot \mathrm{~m}^{2}}{\mathrm{~s}}  \tag{4}\\
\hbar=2 \cdot \pi \cdot Q^{2} \cdot l_{p}  \tag{5}\\
e=\frac{16 \cdot l_{p} \cdot c^{2}}{\alpha \cdot Q^{3}}, \text { units }=\frac{\mathrm{m}^{2}}{\mathrm{~kg} \cdot \mathrm{~s} \cdot \sqrt{(k g} \cdot \mathrm{m} / \mathrm{s})}  \tag{6}\\
\mu_{0}=\frac{\pi^{2} \cdot \alpha \cdot Q^{8}}{32 \cdot l_{p} \cdot c^{5}}  \tag{7}\\
\epsilon_{0}=\frac{32 \cdot l_{p} \cdot c^{3}}{\pi^{2} \cdot \alpha \cdot Q^{8}}  \tag{8}\\
k_{e}=\frac{\pi \cdot \alpha \cdot Q^{8}}{128 \cdot l_{p} \cdot c^{3}} \tag{9}
\end{gather*}
$$

## 3 Planck length $l_{p}$

$l_{p}$ in terms of $Q, \alpha, c$. The magnetic constant $\mu_{0}$ has a fixed value. From eqn. 7

$$
\begin{equation*}
l_{p}=\frac{\pi^{2} \cdot \alpha \cdot Q^{8}}{2^{7} \cdot \mu_{0} \cdot c^{5}} \tag{10}
\end{equation*}
$$

$$
\mu_{0}=4 . \pi \cdot 10^{-7} N / A^{2}
$$

$$
\begin{equation*}
l_{p}=\frac{5^{7} \cdot \pi \cdot \alpha \cdot Q^{8}}{c^{5}} \tag{11}
\end{equation*}
$$

## 4 Reference formulas

Here the formulas and their units are cross referenced with common physics equations.

$$
\begin{aligned}
& \alpha=\frac{2 . h}{\mu_{0} \cdot e^{2} \cdot c} \\
& 22 . \pi \cdot Q^{2} \cdot 2 . \pi \cdot l_{p} \frac{32 \cdot l_{p} \cdot c^{5}}{\pi^{2} \cdot \alpha \cdot Q^{8}} \frac{\alpha^{2} \cdot Q^{6}}{256 \cdot l_{p}^{2} \cdot c^{4}} \frac{1}{c} \\
& \alpha=\alpha \\
& c=\frac{1}{\sqrt{\mu_{0} \cdot \epsilon_{0}}} \\
& \mu_{0} \cdot \epsilon_{0}=\frac{\pi^{2} \cdot \alpha \cdot Q^{8}}{32 \cdot l_{p} \cdot c^{5}} \frac{32 \cdot l_{p} \cdot c^{3}}{\pi^{2} \cdot \alpha \cdot Q^{8}}=\frac{1}{c^{2}} \\
& c=c \\
& R_{\infty}=\frac{m_{e} \cdot e^{4} \cdot \mu_{0}^{2} \cdot c^{3}}{8 . h^{3}} \\
& m_{e} \frac{65536 \cdot l_{p}^{4} \cdot c^{8}}{\alpha^{4} \cdot Q^{12}} \frac{\pi^{4} \cdot \alpha^{2} \cdot Q^{16}}{1024 \cdot l_{p}^{2} \cdot c^{10}} c^{3} \frac{1}{8} \frac{1}{8 \cdot \pi^{3} \cdot Q^{6} \cdot 8 \cdot \pi^{3} \cdot l_{p}^{3}} \\
& R_{\infty}=\frac{m_{e}}{4 . \pi \cdot l_{p} \cdot \alpha^{2} \cdot m_{P}} \\
& E_{n}=-\frac{2 \cdot \pi^{2} \cdot k_{e}^{2} \cdot m_{e} \cdot e^{4}}{h^{2} \cdot n^{2}} \\
& 2 . \pi^{2} \frac{\pi^{2} \cdot \alpha^{2} \cdot Q^{16}}{16384 \cdot l_{p}^{2} \cdot c^{6}} m_{e} \frac{65536 \cdot l_{p}^{4} \cdot c^{8}}{\alpha^{4} \cdot Q^{12}} \frac{1}{4 \cdot \pi^{2} \cdot Q^{4} \cdot 4 \cdot \pi^{2} \cdot l_{p}^{2}} \\
& E_{n}=-\frac{m_{e} \cdot c^{2}}{2 \cdot \alpha^{2} \cdot n^{2}} \\
& q_{p}=\sqrt{4 . \pi . \epsilon_{0} . \hbar . c} \\
& q_{p}=\sqrt{4 \cdot \pi \frac{32 \cdot l_{p} \cdot c^{3}}{\pi^{2} \cdot \alpha \cdot Q^{8}} 2 \cdot \pi \cdot Q^{2} \cdot l_{p} c}=\sqrt{\alpha} \cdot e \\
& r_{e}=\frac{e^{2}}{4 . \pi \cdot \epsilon_{0} \cdot m_{e} \cdot c^{2}} \\
& r_{e}=\frac{256 \cdot l_{p}^{2} \cdot c^{4}}{\alpha^{2} \cdot Q^{6}} \frac{1}{4 \cdot \pi} \frac{\pi^{2} \cdot \alpha \cdot Q^{8}}{32 \cdot l_{p} \cdot c^{3}} \frac{1}{m_{e} \cdot c^{2}}=\frac{l_{p} \cdot m_{P}}{\alpha \cdot m_{e}} \\
& m_{e}=\frac{B^{2} \cdot r^{2} \cdot e}{2 . V}
\end{aligned}
$$

$$
\begin{gather*}
V_{p}=\frac{E_{p}}{e} \\
\frac{B^{2} \cdot r^{2} \cdot e^{2}}{E_{p}}=\frac{\pi^{2} \cdot \alpha^{2} \cdot Q^{10}}{64 \cdot l_{p}^{4} \cdot c^{4}} l_{p}^{2} \frac{256 \cdot l_{p}^{2} \cdot c^{4}}{\alpha^{2} \cdot Q^{6}} \frac{1}{2 \cdot \pi \cdot Q^{2} \cdot c} \\
\frac{B^{2} \cdot r^{2} \cdot e^{2}}{E_{p}}=m_{P} \tag{18}
\end{gather*}
$$

## 5 Electron as magnetic monopole

$m_{e}$ in terms of $m_{P}, t_{p}, \alpha, e, c$.

The ampere-meter is the SI unit for pole strength (the product of charge and velocity) in a magnet (A.m = e.c). A magnetic monopole [2] is a hypothetical particle that is a magnet with only 1 pole. Proposed is a dimensionless geometrical formula for the electron constructed from magnetic monopoles $M_{p o l e}$. Planck mass $=m_{P}$, electron mass $=m_{e}$.

$$
\begin{equation*}
m_{e}=2 \cdot m_{P} \cdot t_{x} \cdot M_{\text {pole }}^{3} \tag{19}
\end{equation*}
$$

where...

$$
\begin{equation*}
M_{\text {pole }}=\frac{2 \cdot \pi^{2}}{3 \cdot \alpha^{2} \cdot e_{x} \cdot c_{x}} \tag{20}
\end{equation*}
$$

the conversion of Planck time $t_{p}$, elementary charge $e$ and speed of light $c$ to $1 s, 1 C, 1 \mathrm{~m} / \mathrm{s}$ requires dimensionless frequencies whose numerical values are equivalent $\left(t_{x}, e_{x}, c_{x}\right)$.

$$
\begin{gathered}
\frac{t_{p}}{t_{x}}=\frac{5.3912 \ldots e^{-44} s}{5.3912 \ldots e^{-44}}=1 s \\
\frac{e}{e_{x}}=\frac{1.6021764 \ldots e^{-19} C}{1.6021764 \ldots e^{-19}}=1 C \\
\frac{c}{c_{x}}=\frac{299792458 \mathrm{~m} / \mathrm{s}}{299792458}=1 \mathrm{~m} / \mathrm{s}
\end{gathered}
$$

## 6 Numerical reference

$\alpha$ in terms of $Q$.
The accepted standard (experimental) values for the physical constants may be referenced from the CODATA website. The CODATA 2010 values:

$$
\begin{aligned}
& R_{\infty}=10973731.568539(55) \\
& h=6.62606957(29) e-34 \text { [4] } \\
& \alpha=137.035999074(44) \\
& l_{p}=1.616199(97) e-35[6] \\
& e=1.602176565(35) e-19[7] \\
& m_{e}=9.10938291(40) e-31[8]
\end{aligned}
$$

$$
\begin{aligned}
& \mu_{0}=4 . \pi .10^{-7} \text { (fixed) } \\
& G=6.67384(80) e-11[10]
\end{aligned}
$$

The Rydberg constant $R$, which incoprorates the other constants, is the most accurately measured fundamental physical constant and so may be used to cross-check the results.

$$
R_{\infty}=\frac{m_{e} \cdot e^{4} \cdot \mu_{0}^{2} \cdot c^{3}}{8 \cdot h^{3}}
$$

Using the CODATA 2010 precision range as a data filter, $\alpha$ and $Q$ as the variables and by replacing Planck length $l_{p}$ with eqn.11, the range of possible solutions for $\alpha$ and $Q$ may be determined.

$$
\begin{aligned}
& \text { for } \alpha=137.0359 \ldots \text { to } 137.0361 \ldots \\
& \text { for } Q=1.019112 \ldots \text { to } 1.019114 \ldots \\
& h=2^{2} * 5^{7} * \pi^{3} * \alpha * Q^{10} / c^{5} \\
& \text { if }(h>\text { hmin and } h<\text { hmax }) \text { then } \\
& R=\pi^{2} * c^{5} /\left(2^{10} * 3^{3} * 5^{21} * \alpha^{8} * Q^{15}\right) \\
& \text { if }(R>\text { rmin and } R<\text { rmax }) \text { then } \\
& e=16 * 5^{7} * \pi * Q^{5} / c^{3} \\
& \text { if }(e>\text { emin and } e<\text { emax }) \text { then } \\
& m_{e}=\left(2 * \pi * Q^{2} / c\right) *\left(\pi^{4} /\left(2^{8} * 3^{3} * 5^{14} * \alpha^{5} * Q^{7}\right)\right) \\
& \text { if }\left(m_{e}>\text { mmin and } m_{e}<\text { mmax }\right) \text { then } \\
& \text { print }(\text { alpha, } Q) \ldots
\end{aligned}
$$

This gives the following range of values for $\alpha$ and $Q$;

$$
\begin{aligned}
& \alpha=137.035997274 \text { (980) } \\
& Q=1.019113418388 \text { (3885) }
\end{aligned}
$$

Note: As the Rydberg numerical precision far exceeds the other constants, generally we can use it to numerically define $Q$ in terms of $\alpha$ with this precision.

$$
\begin{gathered}
x=\alpha^{8} * Q^{15} \\
10973731.568539(55)=\pi^{2} * c^{5} /\left(2^{10} * 3^{3} * 5^{21} * x\right) \\
x=165201929560725953(828000)
\end{gathered}
$$

$$
Q=\left(x * \alpha^{8}\right)^{1 / 15}
$$

## 7 Magnetic (electric) constant

$$
\mu_{0}=4 . \pi \cdot 10^{-7} N / A^{2}
$$

Therefore, in a vacuum, the force per meter of length between the two infinite straight parallel conductors carrying a current of 1 A and spaced apart by 1 m , is exactly $2 \cdot 10^{-7} \mathrm{~N} / \mathrm{m}$

